

Chapter 6

Swapping Elements

- For example, you can sort a list by repeatedly swapping elements that are not in order
- Swap the elements at positions i and j of a list values
- We'd like to set values[i] to values[j]. But that overwrites the value that is currently stored in values[i], so we want to save that first:



Before moving a new value into a location (say blue) copy blue's value elsewhere and then move black's value into blue. Then move the temporary value (originally in blue) into black.

Swapping Elements (2)

- Swapping elements [1] and [3]
 - This sets up the scenario for the actual code that will follows



Swapping Elements (3)





10/5/16

Swapping Elements (4)





Reading Input

• It is very common to read input from a user and store it in a list for later processing.

```
values = []
print("Please enter values, Q to quit:")
userInput = input("")
while userInput.upper() != "Q" :
    values.append(float(userInput))
    userInput = input("")
```

```
Please enter values, Q to quit:
32
29
67.5
Q
```

Example One

• Open the file largest.py in Pycharm

Built-In Operations For Lists

- Use the insert() method to insert a new element at any position in a list
- The in operator tests whether an element is contained in a list
- Use the pop() method to remove an element from any position in a list
- Use the remove() method to remove an element from a list by value
- Two lists can be concatenated using the plus (+) operator
- Use the list() function to copy lists

Built-In Operations For Lists

• Use the slice operator (:) to extract a sublist or substrings

Example Problems

- Open the file largest.py in Wing
- Modify the program to find and print both the largest and smallest number
 - Find the largest number
 - Print the list
 - Print the string " <== largest value" next to the largest number
 - Find the smallest number
 - Print the list
 - Print the string " <== smallest value" next to the smallest number
- Modify the program again
 - Find the largest number
 - Find the smallest number
 - Print the list
 - Print the string " <== largest value" next to the largest number
 - Print the string " <== smallest value" next to the smallest number

Using Lists With Functions

SECTION 6.4

10/5/16

Page 57

Using Lists With Functions

- A function can accept a list as an argument
- The following function visits the list elements, but it does not modify them

```
def sum(values) :
   total = 0
   for element in values :
        total = total + element
   return total
```

Modifying List Elements

• The following function multiplies all elements of a list by a given factor:

```
def multiply(values, factor) :
    for i in range(len(values)) :
        values[i] = values[i] * factor
```

• The parameter variables values and factor are created



- The parameter variables are initialized with the arguments that are passed in the call
- In our case, values is set to scores and factor is set to 10
 - Note that values and scores are references to the *same* list



• The function multiplies all list elements by 10



- The function returns. Its parameter variables are removed
- However, scores still refers to the list with the modified elements



Returning Lists From Functions

- Simply build up the result in the function and return it
- In this example, the squares() function returns a list of squares from 0^2 up to $(n-1)^2$:

```
def squares(n) :
    result = []
    for i in range(n) :
        result.append(i * i)
    return result
```

Example One

- Open the file reverse.py
- This program reads values from the user, multiplies them by 10, and prints them in reverse order
- The readFloats function returns a list
- The multiply function has a list argument, it modifies the list elements
- The printReversed function has a list argument, but it does not modify the list elements

Call By: Value Vs. Reference

- Call by value:
 - When the contents of a variable that was passed to a function can never be changed by that function
- Call by reference:
 - Function can change the arguments of a method call
 - A Python method can mutate the contents of a list when it receives an reference to

Tuples

- A tuple is similar to a list, but once created, its contents cannot be modified (a tuple is an immutable version of a list).
- A tuple is created by specifying its contents as a comma-separated sequence. You can enclose the sequence in parentheses:

triple = (5, 10, 15)

• If you prefer, you can omit the parentheses:

triple = 5, 10, 15

Returning Multiple Values

• It is common practice in Python, however, to use tuples to return multiple values.

```
# Function definition
def readDate() :
    print("Enter a date:")
    month = int(input(" month: "))
    day = int(input(" day: "))
    year = int(input(" year: "))
    return (month, day, year) # Returns a tuple.
# Function call: assign entire value to a tuple
date = readDate()
# Function call: use tuple assignment:
(month, day, year) = readDate()
```

Problem Solving

SECTION 6.5: ADAPTING ALGORITHMS

Adapting Algorithms

- Consider this example problem: You are given the quiz scores of a student. You are to compute the final quiz score, which is the sum of all scores after dropping the lowest one
 - For example, if the scores are

8 7 8.5 9.5 7 5 10

• then the final score is 50

Adapting a Solution

- What steps will we need?
 - Find the minimum
 - Remove it from the list
 - Calculate the sum
- What tools do we know?
 - Finding the minimum value (Section 6.3.4)
 - Removing matches (Section 6.3.7)
 - Calculating the sum (Section 6.4)
- But wait... We need to find the POSITION of the minimum value, not the value itself
 - Hmmm. Time to adapt



Planning a Solution

- Refined Steps:
 - Find the minimum value
 - Find its position
 - Remove it from the list
 - Calculate the sum
- Let's try it
 - Find the position of the minimum:
 - At position 5
 - Remove it from the list
 - Calculate the sum

[0]	[1]	[2]	[3]	[4]	[5]	[6]
8	7	8.5	9.5	7	4	10

[0]	[1]	[2]	[3]	[4]	[5]	[6]
8	7	8.5	9.5	7	4	10

[0]	[1]	[2]	[3]	[4]	[5]
8	7	8.5	9.5	7	10

Adapting the code

• Adapt smallest value to smallest position:

Original algorithm

```
smallest = values[0]
for i in range(1, len(values)) :
    if values[i] < smallest :
        smallest = values[i]</pre>
```

Adapted algorithm

```
smallestPosition = 0
for i in range(1, len(values)) :
    if values[i] < values[smallestPosition] :
        smallestPosition = i</pre>
```

10/5/16

Working Out an Example

Problem Statement: The final quiz score for a student is computed by adding up all of the scores except the lowest two

For example, if the scores are: 8, 4, 7, 9, 9, 7, 5, 10

The final score is 50

We are going develop the algorithm and write a program to compute the final score

Step One

- We want to start with a high level decomposition of the problem:
 - Read the data into a list
 - Process the data
 - Display the results
- We will refer back to the algorithms and list operations to help guide our design. Most of the tasks associated with this problem can be solved by using or adapting one or more of the algorithms
- Our next step in the stepwise refine is to identify the step we need to process the data:
 - 1. Read inputs
 - 2. Remove the minimum
 - 3. Remove the minimum again
 - 4. Calculate the sum

Step Two

- Now we start to determine the algorithms we need
- We have working algorithms for reading the inputs, and calculating the sum
- To remove the minimum value we can find the minimum (we have an algorithm for that) and remove it.
 - It is a bit more efficient to find the position of the minimum value and "pop" that position

Step Three

- Plan the functions we need
 - We can compute the sum with the existing sum function
 - We need a function to read the floating point numbers; readFloats()
 - We need a function to remove the minimum; removeMinimum() (we will call this twice)
- Our main function can be structured as:

```
scores = readFloats()
removeMinimum(scores)
removeMinimum(scores)
total = sum(scores)
print("Final Score : ", total)
```

Step Four

- Assemble and test your code
- Review your code and make sure you handle the "normal" and "exceptional" cases.
 - How do you handle an empty list?
 - A list with a single element?
 - What if you don't find a smallest number?
- Remember in our problem statement we are dropping two grades
- It is not possible to compute a minimum if the list is empty or has a single element
 - In that case we should terminate the program with an error message before attempting to call the remove minimum function
- Develop your test cases, and the expected outputs

Testing

• Develop your test cases, and the expected outputs

Test Case	Expected Output	Comment
8 4 7 8.5 9.5 7 5 10	50	Example case
87779	24	Make sure only two instances of the low score are removed
8 7	0	After removing the two low scores, none remain
(no inputs)	Error	That is not a legal input

scores.py

• Open the file scores.py in Wing

A Second Example

Problem Statement: Our task is to analyze whether a die is fair by counting how often each value (1, 2, 3, 4, 5, 6) appears

Our input will be a series of die toss values

For example, if the scores are: 1, 2, 1, 3, 4, 6, 5, 6

The result is 1: 2; 2: 1; 3: 1; 4: 1; 5: 1; 6: 2

We are going develop the algorithm and write a program to compute and print the frequency of each die value

Step One

- We want to start with a high level decomposition of the problem:
 - Read the die values
 - Count how often the values (1, 2, ..., 6) appear
 - Print the counts
- If we think about this we can simplify; do we need to store the values?
 - We are only counting the number of times each die toss occurs. If we create a list of counter we can read and then discard the inputs
- Our next step in the stepwise refine is to identify the steps we need to process the data:
 - 1. Read input
 - 2. For each input value:
 - 1. Increment the corresponding counter
 - 3. Print the counters

Step Two

- Determine the algorithms we need:
- We don't have an algorithm for reading inputs and incrementing a counter (yet) but it is easy to build one
 - If we have a list of length 6 we can simply

counters[value - 1] = counters[value - 1] + 1

- To make it easier was can can not use the [0] position and have
 counters[value] = counters[value] + 1
- So, if we define counters = [0] * (sides + 1)
- Now we can focus on printing the counters
- We can use a count controlled loop and a format string to print the results

Step Three

- Plan the Functions we need:
 - countInputs(sides) # will count the inputs
 - printCounters(counters) # will print the counters
- The main function calls these functions:

```
counters = countInputs(6)
printCounters(counters)
```

Step Four

- Assemble and test your program:
- When updating a counter we have to make sure we do not generate an boundary error; we have to reject inputs < 1 and > 6

Test Case	Expected Output	Comment
123456	111111	Each number occurs once
123	111000	Numbers that do not appear have a count of "0"
1231234	222100	The counters must be correct
No input	000000	All counters are "0"
01234567	ERROR	Inputs out of bounds

dice.py

• Open the file dice.py

Discovering Algorithms by Manipulating Physical Objects

SECTION 6.6

Page 87

10/5/16

Discovering Algorithms

- Consider this example problem:
 - You are given a list whose size is an even number, and you are to switch the first and the second half
- For example, if the list contains the eight numbers:



• Rearrange it to:

Manipulating Objects

- One useful technique for discovering an algorithm is to manipulate physical objects
- Start by lining up some objects to denote an array
 - Coins, playing cards, or small toys are good choices



• Visualize removing one object



Manipulating Objects

• Visualize inserting one object



• How about swapping two coins?



Manipulating Objects

- Back to our original problem. Which tool(s) to use?
 - How about swapping two coins? Four times?



10/5/16

Develop an Algorithm

Pick two locations (indexes) for the first swap and start a loop









- How can j be set to handle any number of items?
 - (size / 2) • ... if size is 8, j is index 4...

l

Also (size / 2)

• And when do we stop our loop?...

i = 0

j = ... (we'll think about that in a minute) While (don't know yet)

```
Swap elements at positions i and j
i=i+1
```

```
i=i+1
```

```
i = 0
j = length / 2
While (i < length / 2)
   Swap elements at positions i and j
   i=i+1
   j=j+1
```

swaphalves.py

• Open the file swaphalves.py

Tables

SECTION 6.7

10/5/16

Page 94

Tables

- Lists can be used to store data in two dimensions (2D) like a spreadsheet
 - Rows and Columns
 - Also known as a 'matrix'

	Gold	Sllver	Bronze
Canada	0	3	0
Italy	0	0	1
Germany	0	0	1
Japan	1	0	0
Kazakhstan	0	0	1
Russia	3	1	1
South Korea	0	1	0
United States	1	0	1

Figure 10 Figure Skating Medal Counts

Creating Tables

• Here is the code for creating a table that contains 8 rows and 3 columns, which is suitable for holding our medal count data:

```
COUNTRIES = 8
MEDALS = 3
counts = [
     [0,3,0],
     [0, 0, 1],
     [0, 0, 1],
     [1, 0, 0],
     [0, 0, 1],
      [3, 1, 1],
     [0, 1, 0]
     [1, 0, 1]
```

Creating Tables (2)

• This creates a list in which each element is itself another list:



Creating Tables (3)

- Sometimes, you may need to create a table with a size that is too large to initialize with literal values
- First, create a list that will be used to store the individual rows

table = []

Creating Tables (4)

• Then create a new list using replication (with the number of columns as the size) for each row in the table and append it to the list of rows:

```
ROWS = 5
COLUMNS = 20
for i in range(ROWS) :
  row = [0] * COLUMNS
  table.append(row)
```

• The result is a table that consists of 5 rows and 20 columns

Accessing Elements

- Use two index values:
 - Row then column

medalCount = counts[3][1]

- To print
 - Use nested for loops
 - Outer row(i) , inner column(j) :

```
for i in range(COUNTRIES):
    # Process the ith row
    for j in range(MEDALS) :
        # Process the jth column in the ith row
        print("%8d" % counts[i][j], end="")
    print() # Start a new line at the end of the row
```



Locating Neighboring Elements

- Some programs that work with two-dimensional lists need to locate the elements that are adjacent to an element
- This task is particularly common in games
- You are at loc i, j
- Watch out for edges!
 - No negative indexes!
 - Not off the 'board'

[i - 1][j - 1]	[i - 1][j]	[i - 1][j + 1]
[i][j - 1]	[i][j]	[i][j + 1]
[i + 1][j - 1]	[i + 1][j]	[i + 1][j + 1]

Adding Rows and Columns



10/5/16

Using Tables With Functions

• When you pass a table to a function, you will want to recover the dimensions of the table. If values is a table, then:

len(values) is the number of rows

len(values[0]) is the number of columns

• For example, the following function computes the sum of all elements in a table:

```
def sum(values) :
    total = 0
    for i in range(len(values)) :
        for j in range(len(values[0])) :
            total = total + values[i][j]
return total
```

Example

• Open the file medals.py

Summary

Page 105

- A list is a container that stores a sequence of values
- Each individual element in a list is accessed by an integer index i, using the notation list[i]
- A list index must be at least zero and less than the number of elements in the list
- An out-of-range error, which occurs if you supply an invalid list index, can cause your program to terminate
- You can iterate over the index values or the elements of a list

- A list reference specifies the location of a list. Copying the reference yields a second reference to the same list
- A linear search inspects elements in sequence until a match is found
- Use a temporary variable when swapping elements
- Lists can occur as function parameters and return values

- When calling a function with a list argument, the function receives a list reference, not a copy of the list
- A tuple is created as a comma-separated sequence enclosed in parentheses
- By combining fundamental algorithms, you can solve complex programming tasks
- You should be familiar with the implementation of fundamental algorithms so that you can adapt them
- Discover algorithms by manipulating physical objects

- Use a two-dimensional list to store tabular data
- Individual elements in a two-dimensional list are accessed by using two index values, table[i][j]

Built-In Operations For Lists

- Use the insert() method to insert a new element at any position in a list
- The in operator tests whether an element is contained in a list
- Use the pop() method to remove an element from any position in a list
- Use the **remove()** method to remove an element from a list by value
- Two lists can be concatenated using the plus (+) operator
- Use the **list()** function to copy lists

Built-In Operations For Lists

• Use the slice operator (:) to extract a sublist or substrings