Common Error (Floating Point, 2)

- For example, the following code multiplies the square root of 2 by itself.
- Ideally, we expect to get the answer 2:

```
r = math.sqrt(2.0)
if r * r == 2.0 :
   print("sqrt(2.0) squared is 2.0")
else :
   print("sqrt(2.0) squared is not 2.0 but", r * r)
```

```
Output:
sqrt(2.0) squared is not 2.0 but 2.0000000000000004
```

The Use of EPSILON

- Use a very small value to compare the difference to determine if floating-point values are '*close enough*'
  - The magnitude of their difference should be less than some threshold
  - Mathematically, we would write that x and y are close enough if:

$$|x - y| < \varepsilon$$

```
EPSILON = 1E-14
r = math.sqrt(2.0)
if abs(r * r - 2.0) < EPSILON :
   print("sqrt(2.0) squared is approximately 2.0")
```

Lexicographical Order

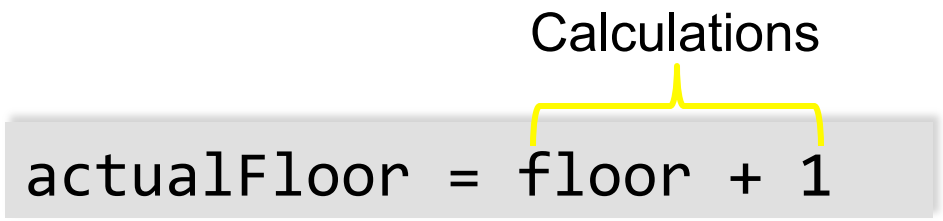
- To compare Strings in ‘dictionary’ like order:

  string1 < string2

- Notes
  - All UPPERCASE letters come before lowercase
  - ‘space’ comes before all other printable characters
  - Digits (0-9) come before all letters
  - See Appendix A for the Basic Latin (ASCII) Subset of Unicode

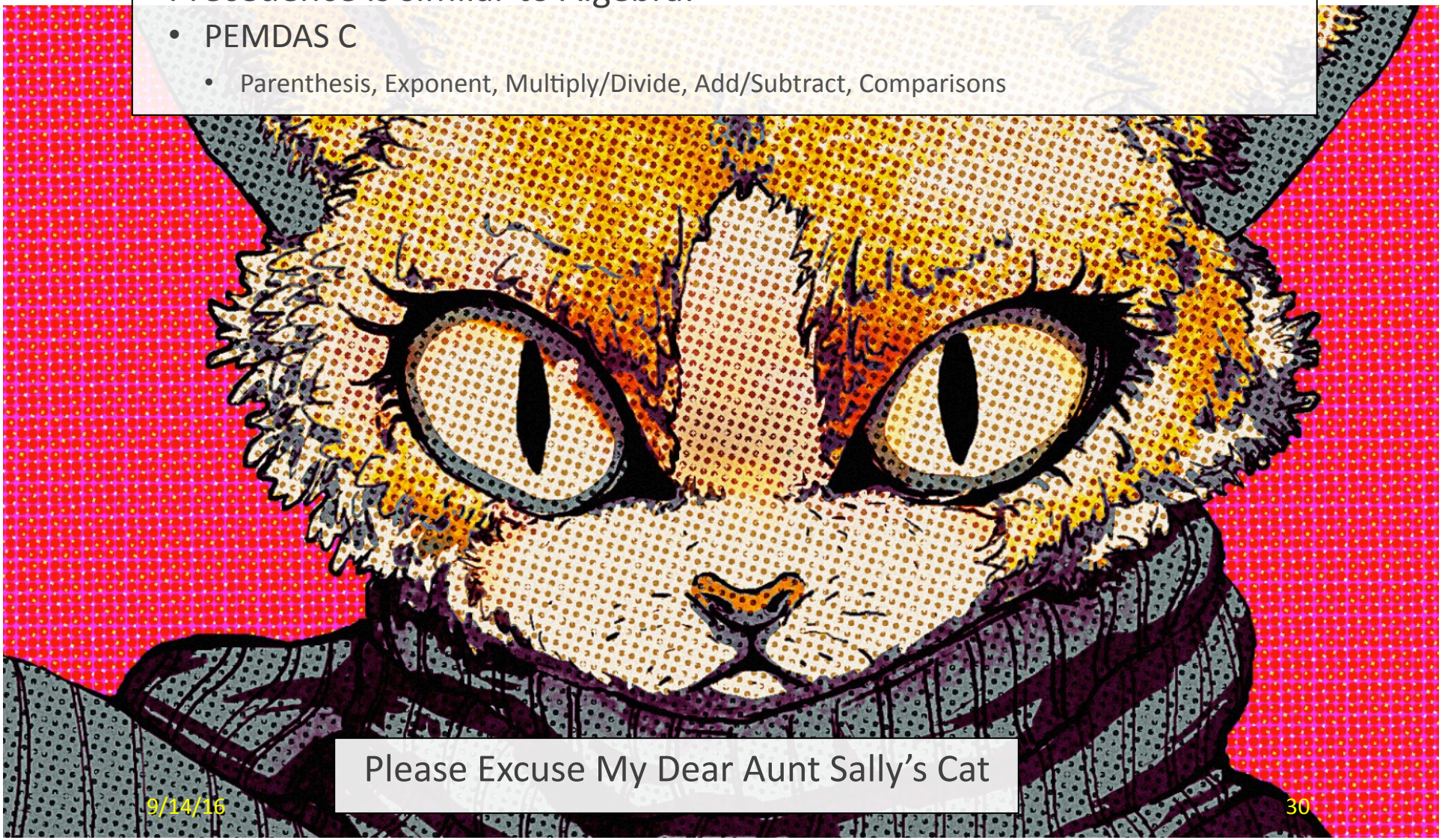
Operator Precedence

- The comparison operators have lower precedence than arithmetic operators
  - ***Calculations are done before the comparison***
  - Normally your calculations are on the 'right side' of the comparison or assignment operator



Precedence

- Precedence is similar to Algebra:
  - PEMDAS C
    - Parenthesis, Exponent, Multiply/Divide, Add/Subtract, Comparisons



Please Excuse My Dear Aunt Sally's Cat

A Third Example

- The university bookstore has a Kilobyte Day sale every October 24 (10.24), giving an 8 percent discount on all computer accessory purchases if the price is less than $128, and a 16 percent discount if the price is at least $128.

Implementing an `if` Statement (1)

1) Decide on a branching condition

```
original price < 128?
```

2) Write pseudocode for the true branch

```
discounted price = 0.92 x original price
```

3) Write pseudocode for the false branch

```
discounted price = 0.84 x original price
```

Implementing an `if` Statement (2)

4) Double-check relational operators

- Test values below, at, and above the comparison (127, 128, 129)

5) Remove duplication

discounted price = ____ x original price

6) Test both branches

discounted price = 0.92 x 100 = 92

discounted price = 0.84 x 200 = 168

Implementing an `if` Statement (3)

7. Write the code in Python

A Third Example

- The university bookstore has a Kilobyte Day sale every October 24 (10.24), giving an 8 percent discount on all computer accessory purchases if the price is less than $128, and a 16 percent discount if the price is at least $128.

```
if originalPrice < 128 :
   discountRate = 0.92
else :
   discountRate = 0.84
discountedPrice = discountRate * originalPrice
```

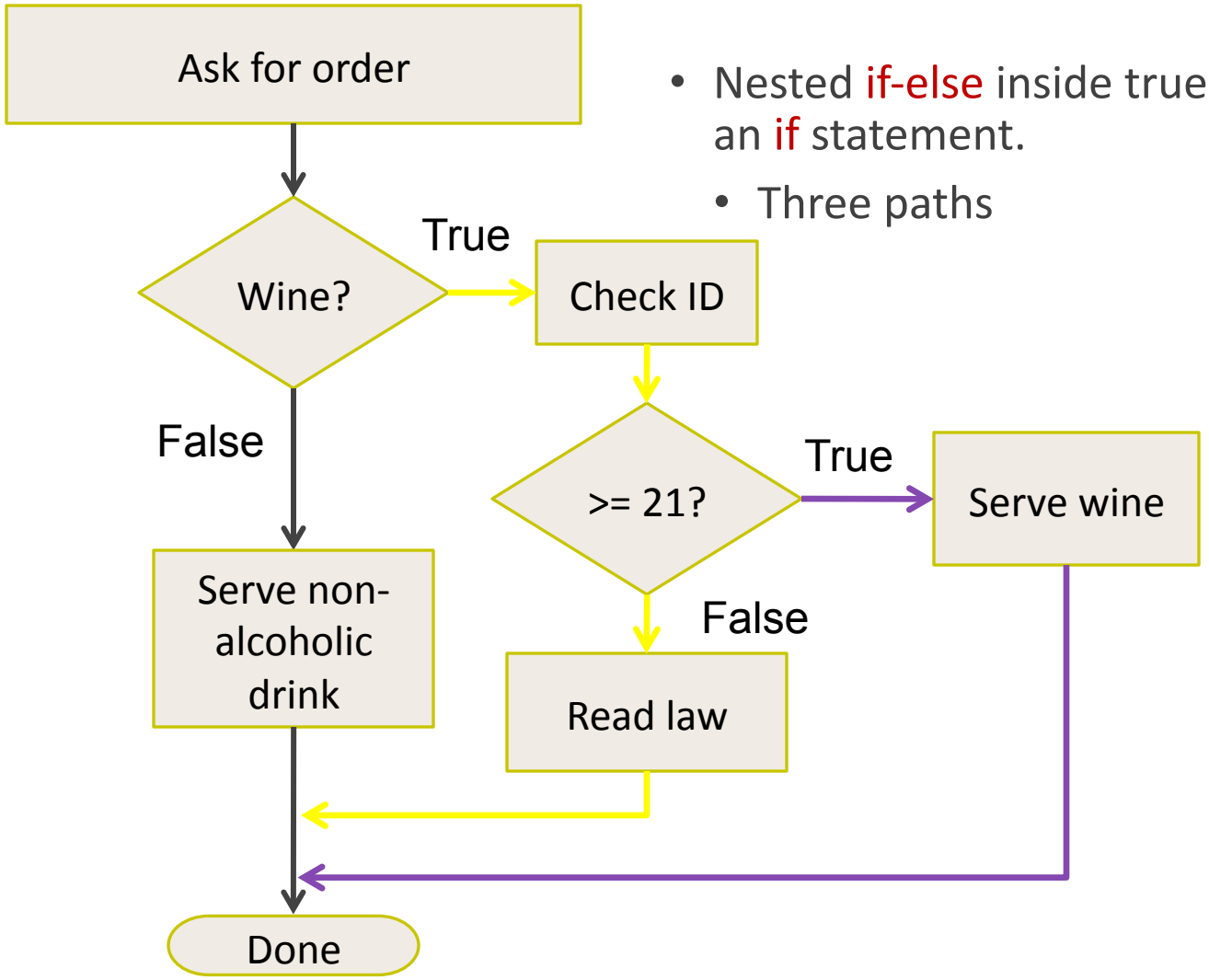
The Sale Example

- Open the file:
  - sale.py
- Run the program several time using different values
  - Use values less than 128
  - Use values greater that 128
  - Enter 128
- What results do you get?

Nested Branches

- You can *nest* an if inside either branch of an if statement.
- Simple example: Ordering drinks
  - Ask the customer for their drink order
  - `if` customer orders wine
    - Ask customer for ID
    - `if` customer's age is 21 or over
      - Serve wine
    - Else
      - Politely explain the law to the customer
  - Else
    - Serve customers a non-alcoholic drink

Flowchart of a Nested if



- Nested if-else inside true branch of an if statement.
  - Three paths

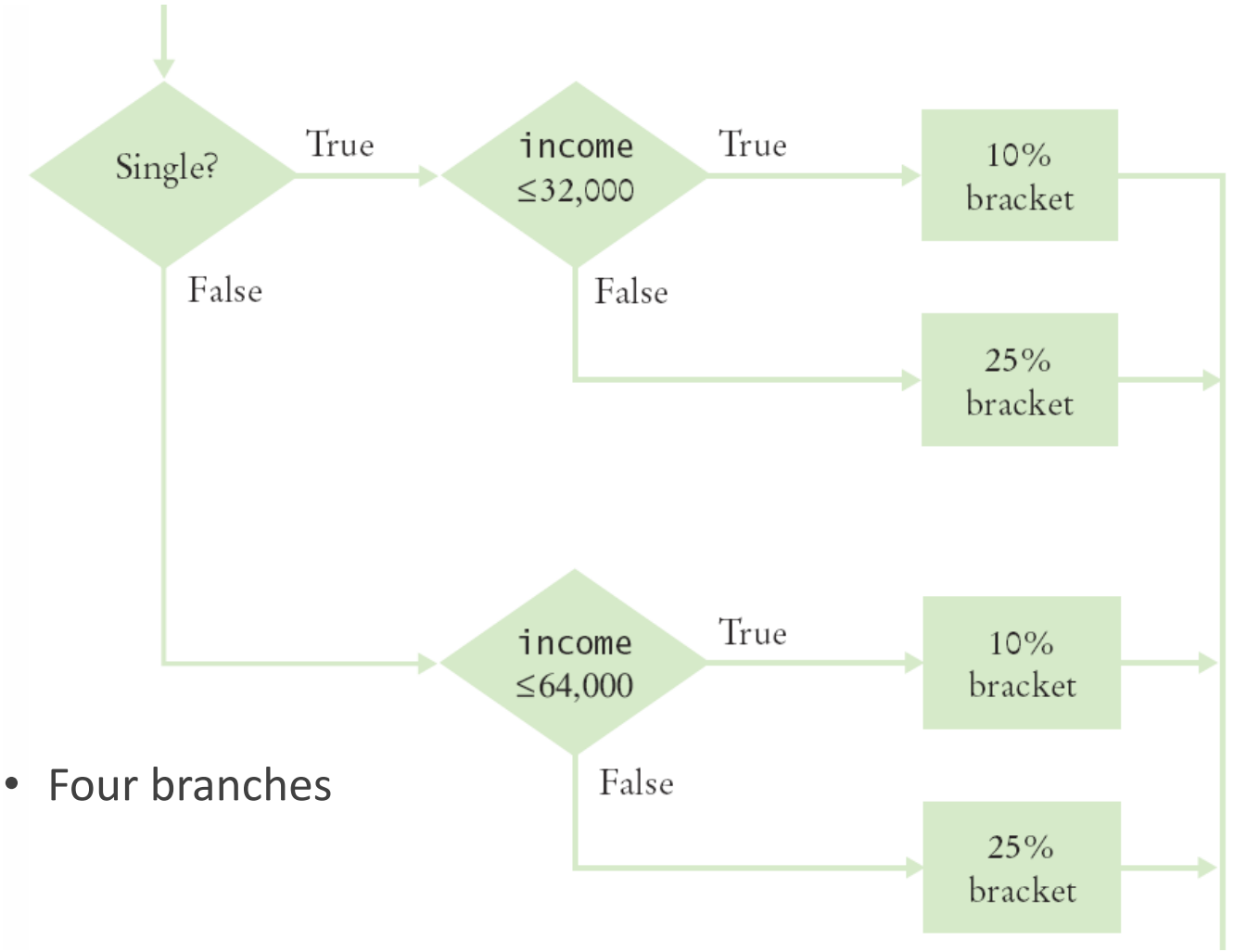
Tax Example: nested `if`s

- Four outcomes (branches)

- Single
  - <= 32000
  - > 32000
- Married
  - <= 64000
  - > 64000

Table 3 Federal Tax Rate Schedule		
If your status is Single and if the taxable income is	the tax is	of the amount over
at most $32,000	10%	$0
over $32,000	$3,200 + 25%	$32,000
If your status is Married and if the taxable income is	the tax is	of the amount over
at most $64,000	10%	$0
over $64,000	$6,400 + 25%	$64,000

Flowchart for the Tax Example



- Four branches

Taxes.py (1)

```
1  ##
2  #  This program computes income taxes, using a simplified tax schedule.
3  #
4
5  # Initialize constant variables for the tax rates and rate limits.
6  RATE1 = 0.10
7  RATE2 = 0.25
8  RATE1_SINGLE_LIMIT = 32000.0
9  RATE1_MARRIED_LIMIT = 64000.0
10
11 # Read income and marital status.
12 income = float(input("Please enter your income: "))
13 maritalStatus = input("Please enter s for single, m for married: ")
14
15 # Compute taxes due.
16 tax1 = 0.0
17 tax2 = 0.0
18
19 if maritalStatus == "s" :
20    if income <= RATE1_SINGLE_LIMIT :
21       tax1 = RATE1 * income
22    else :
23       tax1 = RATE1 * RATE1_SINGLE_LIMIT
24       tax2 = RATE2 * (income - RATE1_SINGLE_LIMIT)
25 else :
26    if income <= RATE1_MARRIED_LIMIT :
27       tax1 = RATE1 * income
28    else :
29       tax1 = RATE1 * RATE1_MARRIED_LIMIT
30       tax2 = RATE2 * (income - RATE1_MARRIED_LIMIT)
31
32 totalTax = tax1 + tax2
33
```

Taxes.py (2)

- The ‘True’ branch (Single)
  - Two branches within this branch

```
19  if maritalStatus == "s" :
20      if income <= RATE1_SINGLE_LIMIT :
21          tax1 = RATE1 * income
22      else :
23          tax1 = RATE1 * RATE1_SINGLE_LIMIT
24          tax2 = RATE2 * (income - RATE1_SINGLE_LIMIT)
```

Taxes.py (3)

- The ‘False’ branch (Married)

```
else :
    if income <= RATE1_MARRIED_LIMIT :
        tax1 = RATE1 * income
    else :
        tax1 = RATE1 * RATE1_MARRIED_LIMIT
        tax2 = RATE2 * (income - RATE1_MARRIED_LIMIT)
```

Running the Tax Example

- Open the file:
  - taxes.py
- Run the program several time using different values for income and marital status
  - Use income values less than $32,000
  - Use income values greater than $64,000
  - Enter “&” as the marital status
- What results do you get?

Hand-tracing

- Hand-tracing helps you understand whether a program works correctly
- Create a table of key variables
  - Use pencil and paper to track their values
- Works with pseudocode or code
  - Track location with a marker
- Use example input values that:
  - You know what the correct outcome should be
  - Will test each branch of your code

Hand-tracing the Tax Example

tax1	tax2	income	marital status
0	0		

- Setup
  - Table of variables
  - Initial values

```
6   RATE1 = 0.10
7   RATE2 = 0.25
8   RATE1_SINGLE_LIMIT = 32000.0
9   RATE1_MARRIED_LIMIT = 64000.0

15  # Compute taxes due.
16  tax1 = 0.0
17  tax2 = 0.0
```

Hand-tracing the Tax Example (2)

tax1	tax2	income	marital status
0	0	80000	m

- Input variables
  - From user
  - Update table

```
11  # Read income and marital status.
12  income = float(input("Please enter your income: "))
13  maritalStatus = input("Please enter s for single, m for married: ")
```

- Because marital status is not “s” we skip to the else on line 25

```
19  if maritalStatus == "s" :

25  else :
```

Hand-tracing the Tax Example (3)

- Because income is not <= 64000, we move to the else clause on line 28
  - Update variables on lines 29 and 30
  - Use constants

```
26      if income <= RATE1_MARRIED_LIMIT :
27         tax1 = RATE1 * income
28      else :
29         tax1 = RATE1 * RATE1_MARRIED_LIMIT
30         tax2 = RATE2 * (income - RATE1_MARRIED_LIMIT)
```

tax1	tax2	income	marital status
~~0~~	~~0~~	80000	m
6400	4000		

Incremental Code and Test

- Implement a solution to one input
  - Test it
- Add a solution to a second input
  - Test it
- Think a little more about whether there is a clever way to add more solutions
- Add solutions incrementally
  - Test them
- It's okay if it breaks at first
  - Go back and understand why it's breaking
  - Code doesn't work for a specific reason – it's not arbitrary

Multiple Alternatives

3.4 Multiple Alternatives

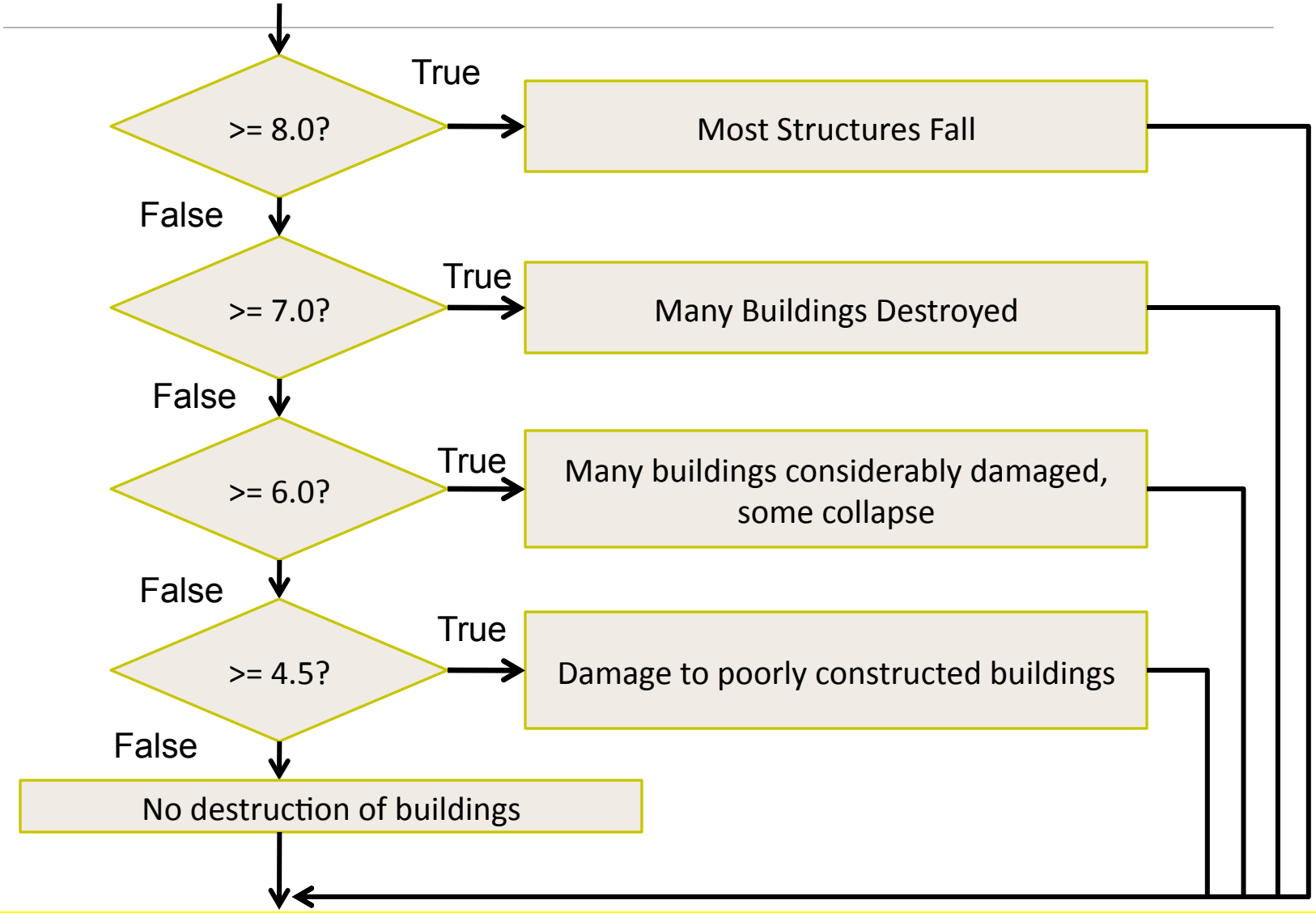
- What if you have more than two branches?
- Count the branches for the following earthquake effect example:
  - 8 (or greater)
  - 7 to 7.99
  - 6 to 6.99
  - 4.5 to 5.99
  - Less than 4.5

When using multiple `if` statements, test the general conditions after the more specific conditions.

Table 4 Richter Scale

Value	Effect
8	Most structures fall
7	Many buildings destroyed
6	Many buildings considerably damaged, some collapse
4.5	Damage to poorly constructed buildings

Flowchart of Multiway Branching



`elif` Statement

- Short for Else, if…
- As soon as one on the test conditions succeeds, the statement block is executed
  - No other tests are attempted
- If none of the test conditions succeed the final else clause is executed

`if, elif` Multiway Branching

```
if richter >= 8.0 :   # Handle the ‘special case’ first
   print("Most structures fall")
elif richter >= 7.0 :
   print("Many buildings destroyed")
elif richter >= 6.0 :
   print("Many buildings damaged, some collapse")
elif richter >= 4.5 :
   print("Damage to poorly constructed buildings")
else :    # so that the ‘general case’ can be handled last
   print("No destruction of buildings")
```

What is Wrong With This Code?

```
if richter >= 8.0 :
   print("Most structures fall")
if richter >= 7.0 :
   print("Many buildings destroyed")
if richter >= 6.0 :
   print("Many buildings damaged, some collapse")
if richter >= 4.5 :
   print("Damage to poorly constructed buildings")
```

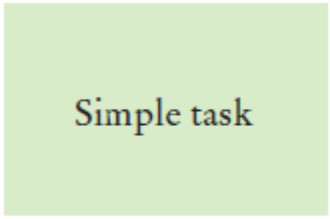
earthquake Example

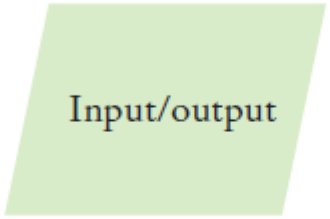
- Open the file:
  - earthquake.py
- Run the program with several different inputs

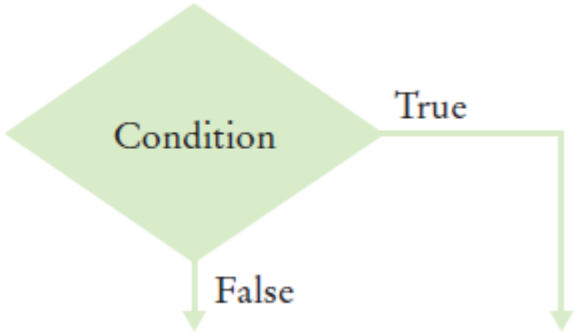
Using Flowcharts to Develop and Refine Algorithms

3.5 Problem Solving: Flowcharts

- You have seen a few basic flowcharts
- A flowchart shows the structure of decisions and tasks to solve a problem
- Basic flowchart elements:







- Connect them with arrows
  - But never point an arrow inside another branch!

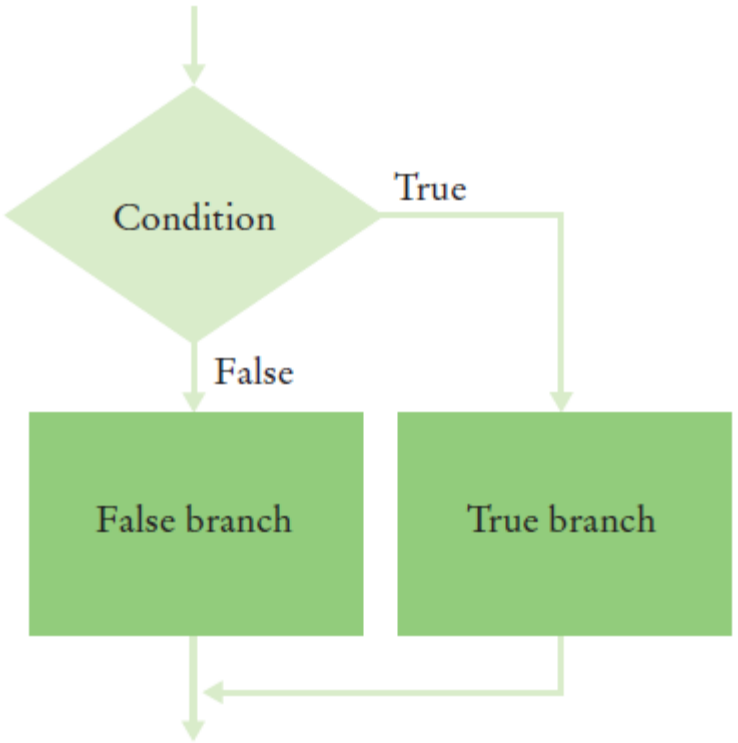
Each branch of a decision can contain tasks and further decisions

Using Flowcharts

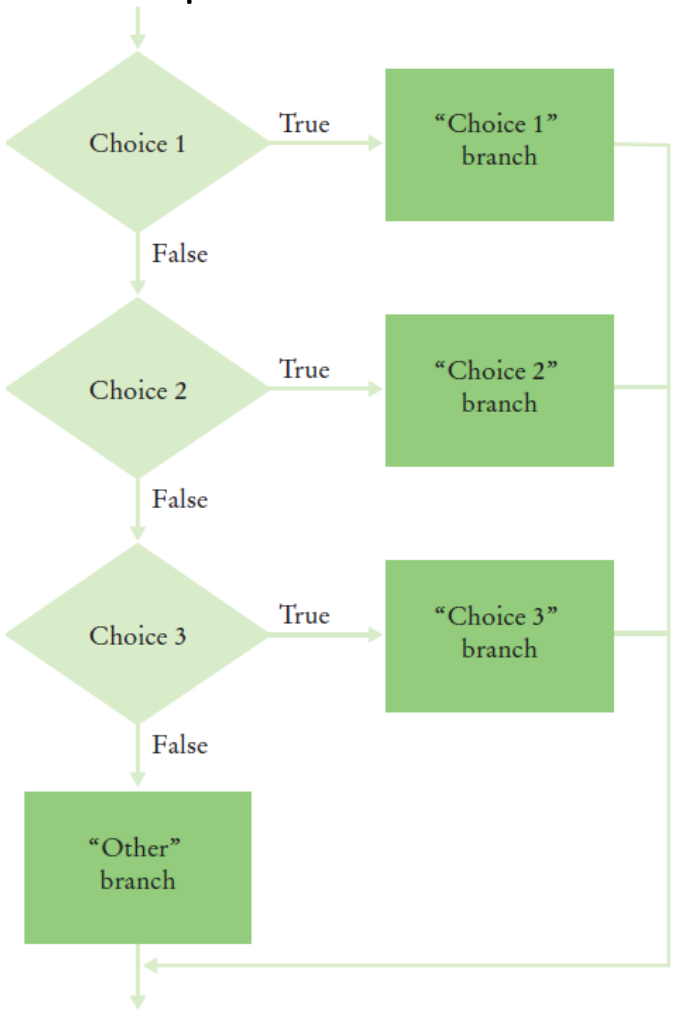
- Flowcharts are an excellent tool
- They can help you visualize the flow of your algorithm
- Building the flowchart
  - Link your tasks and input / output boxes in the sequence they need to be executed
  - When you need to make a decision use the diamond (a conditional statement) with two outcomes
  - Never point an arrow inside another branch

Conditional Flowcharts

Two Outcomes



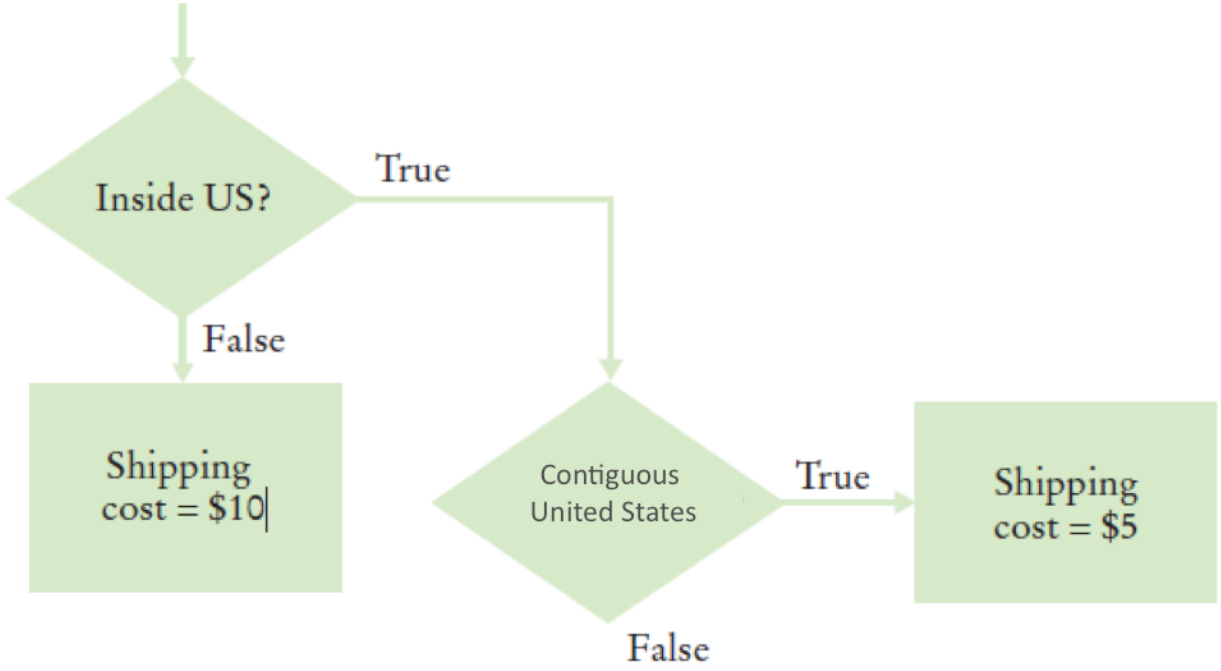
Multiple Outcomes



Shipping Cost flowchart

Shipping costs are $5 inside the contiguous the United States (Lower 48 states), and $10 to Hawaii and Alaska. International shipping costs are also $10.

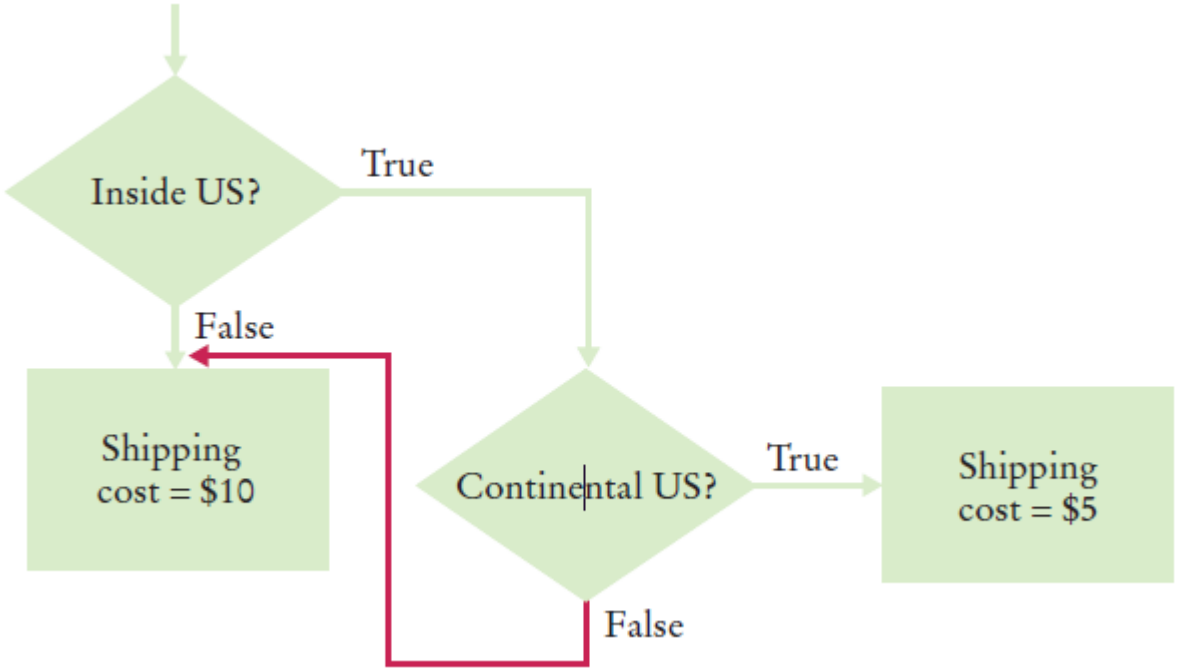
- Three Branches:



Don’t Connect Branches!

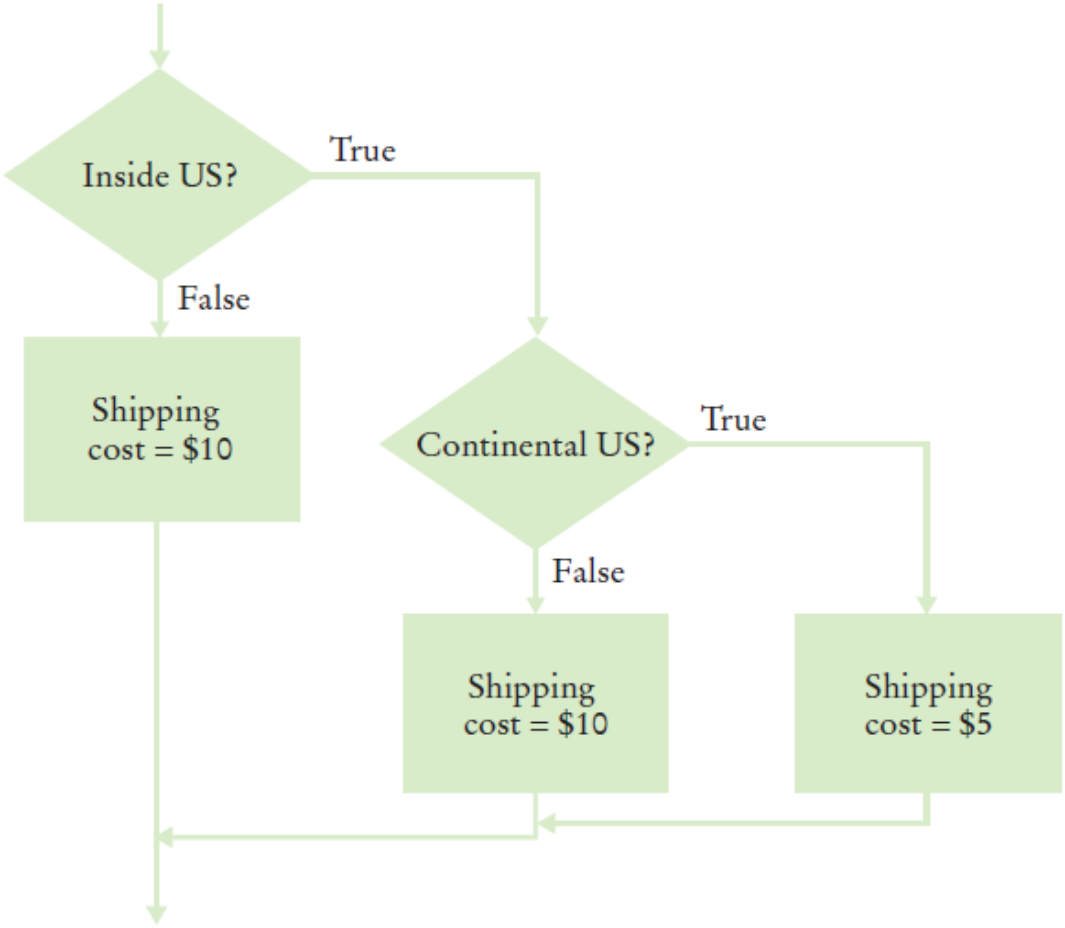
Shipping costs are $5 inside the United States, except that to Hawaii and Alaska they are $10. International shipping costs are also $10.

- Don’t do this!



Shipping Cost Flowchart

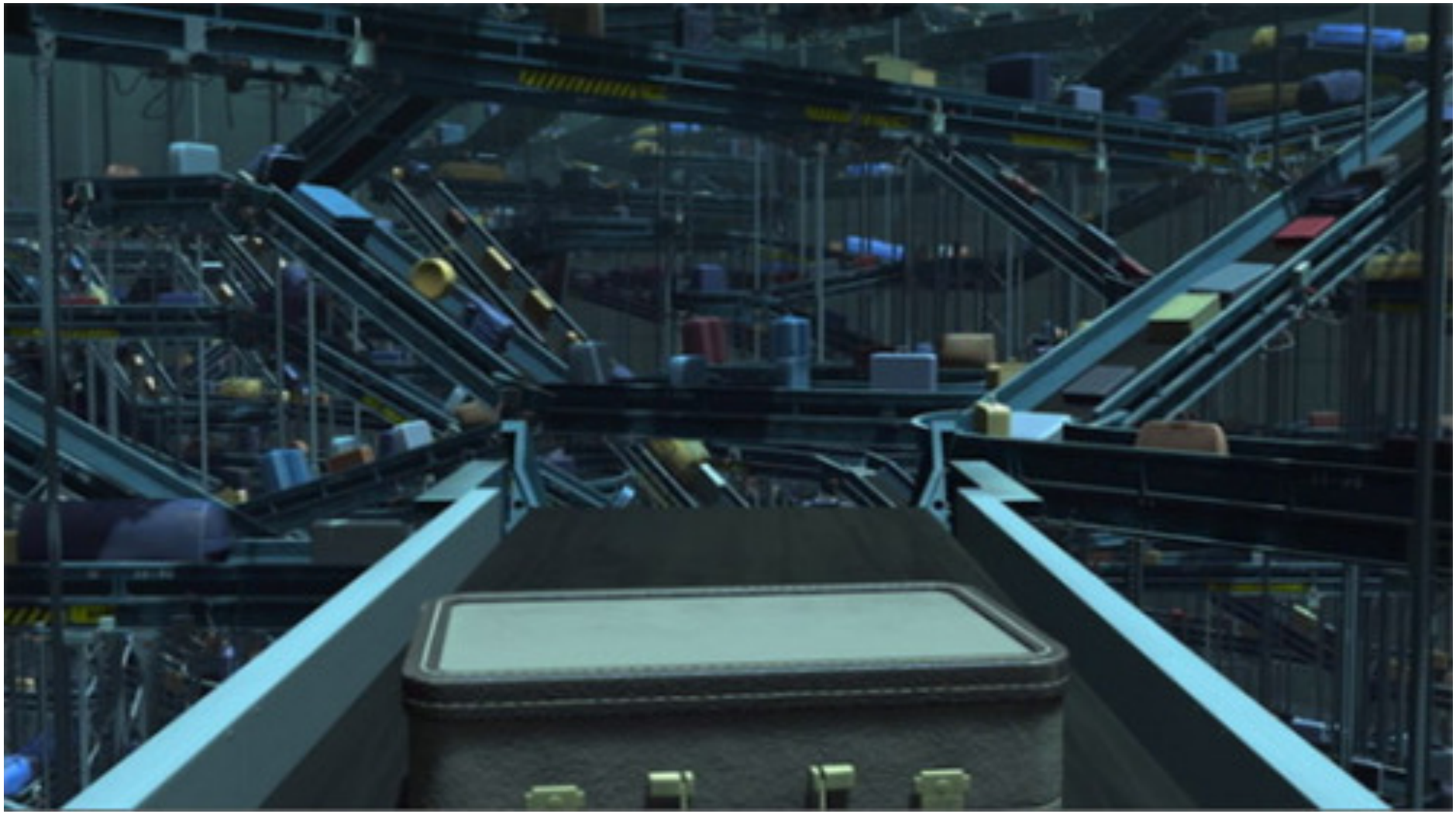
Shipping costs are $5 inside the United States, except that to Hawaii and Alaska they are $10. International shipping costs are also $10.



Shipping Example

- Open the file:
  - Shipping.py
- Run the program with several different inputs?
  - What happens if you enter “usa” as the country?
- We will learn several ways to correct the code later in this chapter

Complex Decision Making is Hard



Building Test Cases

Problem Solving: Test Cases

- Aim for complete coverage of all decision points:
  - There are two possibilities for the marital status and two tax brackets for each status, yielding four test cases
  - Test a handful of boundary conditions, such as an income that is at the boundary between two tax brackets, and a zero income
  - If you are responsible for error checking (which is discussed in Section 3.9), also test an invalid input, such as a negative income
- Each branch of your code should be covered with a test case

Choosing Test Cases

- Choose input values that:
  - Test boundary cases and 0 values
  - Test each branch

Test Case	Expected Output	Comment
30,000 s	3,000	10% bracket
72,000 s	13,200	3,200 + 25% of 40,000
50,000 m	5,000	10% bracket
104,000 m	16,400	6,400 + 25% of 40,000
32,000 s	3,200	boundary case
0 s	0	boundary case

Make a Schedule…

- Make a reasonable estimate of the time it will take you to:
  - Design the algorithm
  - Develop test cases
  - Translate the algorithm to code and enter the code
  - Test and debug your program
- Leave some extra time for unanticipated problems

As you gain more experience your estimates will become more accurate. It is better to have some extra time than to be late

Boolean Variables and Operators

Boolean Variables

- Boolean Variables
  - A Boolean variable is often called a flag because it can be either up (`true`) or down (`false`)
  - boolean is a Python data type
    - `failed = True`
  - Boolean variables can be either `True` or `False`
- There are two Boolean Operators: `and, or`
  - They are used to combine multiple conditions

Combined Conditions: and

- Combining two conditions is often used in range checking
  - Is a value between two other values?
- Both sides of the *and* must be true for the result to be true

```
if temp > 0 and temp < 100 :
   print("Liquid")
```

A	B	A and B
True	True	True
True	False	False
False	True	False
False	False	False

Combined Conditions: or

- We use or if only one of two conditions need to be true
  - Use a compound conditional with an or:

```
if temp <= 0 or temp >=
   100 :
    print("Not liquid")
```

- If either condition is true
  - The result is true

A	B	A or B
True	True	True
True	False	True
False	True	True
False	False	False

The *not* operator: not

- If you need to invert a boolean variable or comparison, precede it with not

```
if not attending or grade < 60 :
   print("Drop?")
```

```
if attending and not(grade < 60) :
   print("Stay")
```

A	not A
True	False
False	True

- If you are using not, try to use simpler logic:

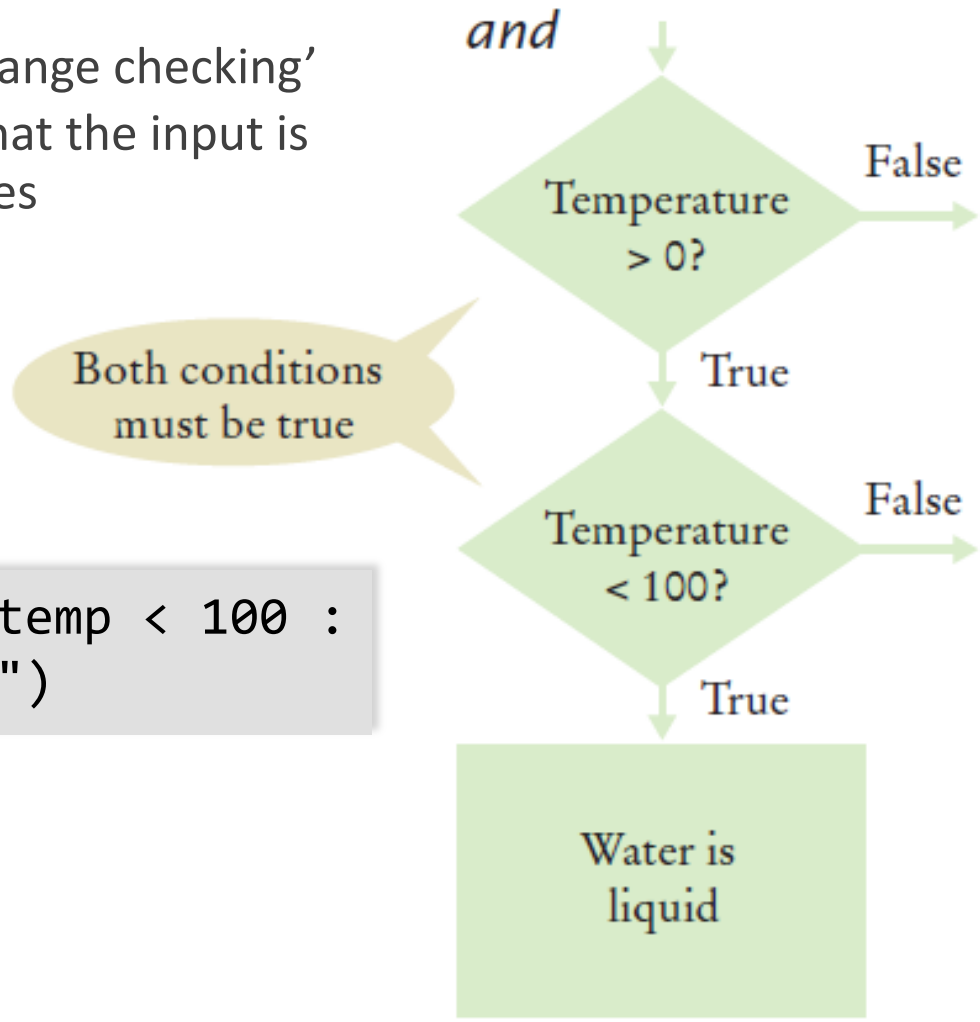
```
if attending and grade >= 60 :
   print("Stay")
```

The *not* operator: inequality !

- A slightly different operator is used for the `not` when checking for inequality rather than negation.
- Example inequality:
  - The password that the user entered is not equal to the password on file.
  - `if userPassword != filePassword :`

and Flowchart

- This is often called ‘range checking’
  - Used to validate that the input is between two values

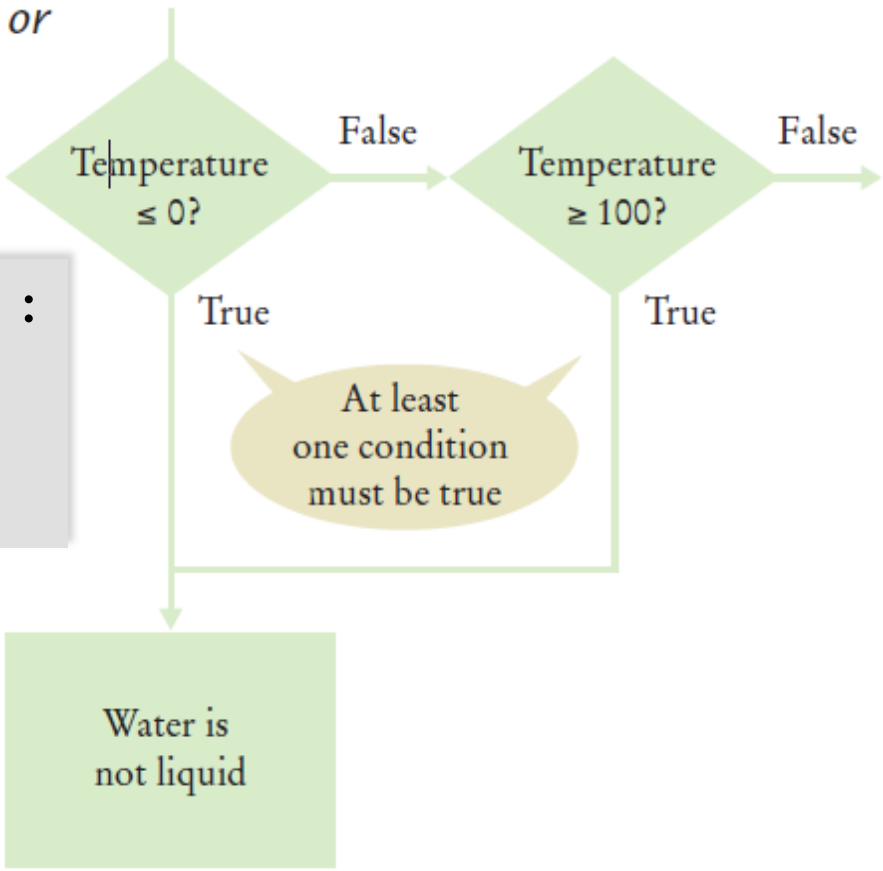



```
if temp > 0 and temp < 100 :
   print("Liquid")
```

or flowchart

- Another form of 'range checking'
  - Checks if value is outside a range

```
if temp <= 0 or temp >= 100 :
   print("Not Liquid")
```



Comparison Example

- Open the file:
  - Compare2.py
- Run the program with several inputs

Boolean Operator Examples

Table 5 Boolean Operator Examples

Expression	Value	Comment
`0 < 200 and 200 < 100`	`False`	Only the first condition is true.
`0 < 200 or 200 < 100`	`True`	The first condition is true.
`0 < 200 or 100 < 200`	`True`	The `or` is not a test for "either-or". If both conditions are true, the result is true.
`0 < x and x < 100 or x == -1`	`(0 < x and x < 100) or x == -1`	The `and` operator has a higher precedence than the `or` operator (see Appendix B).
`not (0 < 200)`	`False`	`0 < 200` is `true`, therefore its negation is `false`.
`frozen == True`	`frozen`	There is no need to compare a Boolean variable with `True`.
`frozen == False`	`not frozen`	It is clearer to use `not` than to compare with `False`.

Common Errors with Boolean Conditions

Confusing `and` and `or` Conditions

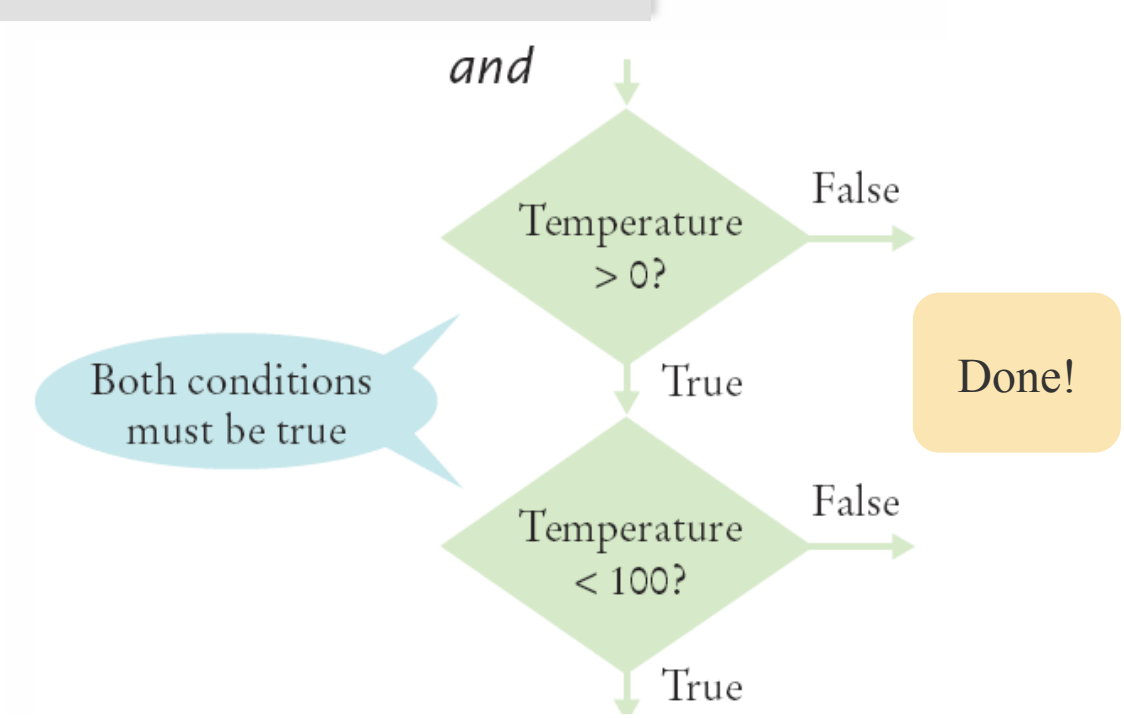
- It is a surprisingly common error to confuse `and` and `or` conditions.
- A value lies between 0 and 100 if it is at least 0 ***and*** at most 100.
- It lies outside that range if it is less than 0 ***or*** greater than 100.

- There is no golden rule; you just have to think carefully.

Short-circuit Evaluation: and

- Combined conditions are evaluated from left to right
  - If the left half of an *and* condition is false, why look further?

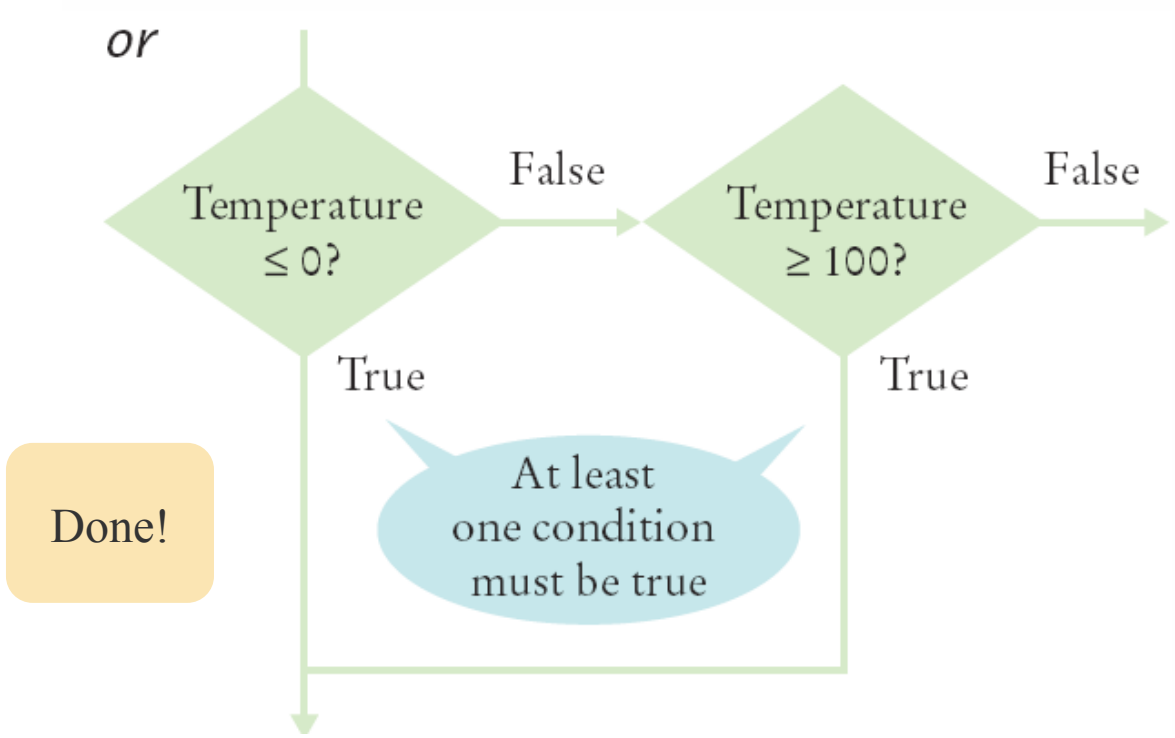
```
if temp > 0 and temp < 100 :
   print("Liquid")
```



Short-circuit evaluation: or

- If the left half of the *or* is true, why look further?

```
if temp <= 0 or temp >= 100 :
   print("Not Liquid")
```



De Morgan's law

- De Morgan's law tells you how to negate and and or conditions:
  - not(A and B) is the same as (not A) or (not B)
  - not(A or B) is the same as (not A) and (not B)
- Example: Shipping is higher to AK and HI

```
if (country != "USA"
   and state != "AK"
   and state != "HI") :
   shippingCharge = 20.00
```

```
if not(country=="USA"
  or state=="AK"
  or state=="HI") :
   shippingCharge = 20.00
```

- To simplify conditions with negations of *and* or *or* expressions, it's a good idea to apply De Morgan's law to move the negations to the innermost level.

Analyzing Strings

Analyzing Strings – The **in** Operator

- Sometimes it's necessary to analyze or ask certain questions about a particular string.
  - Sometimes it is necessary to determine if a string contains a given substring. That is, one string contains an exact match of another string.
  - Given this code segment,

    ```
    name = "John Wayne"
    ```

  - the expression

    ```
    "Way" in name
    ```

  - yields `True` because the substring `"Way"` occurs within the string stored in variable name.
  - The **`not in`** operator is the inverse on the in operator

Substring: Suffixes

- Suppose you are given the name of a file and need to ensure that it has the correct extension

```
if filename.endswith(".html") :
    print("This is an HTML file.")
```

- The `endswith()` string method is applied to the string stored in filename and returns `True` if the string ends with the substring ".html" and `False` otherwise.

Operations for Testing Substrings

Table 6 Operations for Testing Substrings

Operation	Description
substring `in` *s*	Returns `True` if the string *s* contains *substring* and `False` otherwise.
s`.count(`*substring*`)`	Returns the number of non-overlapping occurrences of *substring* in the string *s*.
s`.endswith(`*substring*`)`	Returns `True` if the string *s* ends with the `substring` and `False` otherwise.
s`.find(`*substring*`)`	Returns the lowest index in the string *s* where *substring* begins, or –1 if *substring* is not found.
s`.startswith(`*substring*`)`	Returns `True` if the string *s* begins with *substring* and `False` otherwise.

Methods: Testing String Characteristics (1)

Table 7 Methods for Testing String Characteristics

Method	Description
`s.isalnum()`	Returns `True` if string *s* consists of only letters or digits and it contains at least one character. Otherwise it returns `False`.
`s.isalpha()`	Returns `True` if string *s* consists of only letters and contains at least one character. Otherwise it returns `False`.
`s.isdigit()`	Returns `True` if string *s* consists of only digits and contains at least one character. Otherwise, it returns `False`.

Methods for Testing String Characteristics (2)

Table 7 Methods for Testing String Characteristics

`s.islower()`	Returns `True` if string *s* contains at least one letter and all letters in the string are lowercase. Otherwise, it returns `False`.
`s.isspace()`	Returns `True` if string *s* consists of only white space characters (blank, newline, tab) and it contains at least one character. Otherwise, it returns `False`.
`s.isupper()`	Returns `True` if string *s* contains at least one letter and all letters in the string are uppercase. Otherwise, it returns `False`.

Comparing and Analyzing Strings (1)

Table 8 Comparing and Analyzing Strings

Expression	Value	Comment
`"John" == "John"`	`True`	`==` is also used to test the equality of two strings.
`"John" == "john"`	`False`	For two strings to be equal, they must be identical. An uppercase "J" does not equal a lowercase "j".
`"john" < "John"`	`False`	Based on lexicographical ordering of strings an uppercase "J" comes before a lowercase "j" so the string `"john"` follows the string `"John"`. See Special Topic 3.2 on page 101.
`"john" in "John Johnson"`	`False`	The substring `"john"` must match exactly.
`name = "John Johnson"` `"ho" not in name`	`True`	The string does not contain the substring `"ho"`.
`name.count("oh")`	`2`	All non-overlapping substrings are included in the count.
`name.find("oh")`	`1`	Finds the position or string index where the first substring occurs.
`name.find("ho")`	`-1`	The string does not contain the substring `ho`.
`name.startswith("john")`	`False`	The string starts with `"John"` but an uppercase "J" does not match a lowercase "j".
`name.isspace()`	`False`	The string contains non-white space characters.
`name.isalnum()`	`False`	The string also contains blank spaces.
`"1729".isdigit()`	`True`	The string only contains characters that are digits.
`"-1729".isdigit()`	`False`	A negative sign is not a digit.

Comparing and Analyzing Strings (2)

Table 8 Comparing and Analyzing Strings

`name.startswith("john")`	`False`	The string starts with `"John"` but an uppercase "J" does not match a lowercase "j".
`name.isspace()`	`False`	The string contains non-white space characters.
`name.isalnum()`	`False`	The string also contains blank spaces.
`"1729".isdigit()`	`True`	The string only contains characters that are digits.
`"-1729".isdigit()`	`False`	A negative sign is not a digit.

Substring Example

- Open the file:
  - Substrings.ph
- Run the program and test several strings and substrings

Input Validation

Input Validation

- Accepting user input is dangerous
  - Consider the Elevator program:
  - Assume that the elevator panel has buttons labeled 1 through 20 (but not 13).

Input Validation

- The following are illegal inputs:
  - The number 13

```
if floor == 13 :
    print("Error: There is no thirteenth floor.")
```

  - Zero or a negative number
  - A number larger than 20

```
if floor <= 0 or floor > 20 :
    print("Error: The floor must be between 1 and 20.")
```

  - An input that is not a sequence of digits, such as five:
    - Python's exception mechanism is needed to help verify integer and floating point values (Chapter 7).

Elevatorsim2.py

```
1  ##
2  #  This program simulates an elevator panel that skips the 13th floor,
3  #   checking for input errors.
4  #
5
6  # Obtain the floor number from the user as an integer.
7  floor = int(input("Floor: "))
8
9  # Make sure the user input is valid.
10 if floor == 13 :
11    print("Error: There is no thirteenth floor.")
12 elif floor <= 0 or floor > 20 :
13    print("Error: The floor must be between 1 and 20.")
14 else :
15    # Now we know that the input is valid.
16    actualFloor = floor
```

Elevator Simulation

- Open the file:
  - elevatorsim2.py
- Test the program with a range of inputs including:
  - 12
  - 14
  - 13
  - -1
  - 0
  - 23
  - 19

Chapter Three Review

Summary: `if` Statement

- The if statement allows a program to carry out different actions depending on the nature of the data to be processed.
- Relational operators (`< <= > >= == !=`) are used to compare numbers and `Strings`.
- `Strings` are compared in lexicographic order.
- Multiple `if` statements can be combined to evaluate complex decisions.
- When using multiple `if` statements, test general conditions after more specific conditions.

Summary: Flowcharts and Testing

- When a decision statement is contained inside the branch of another decision statement, the statements are *nested.*
- Nested decisions are required for problems that have two levels of decision making.
- Flow charts are made up of elements for tasks, input/output, and decisions.
- Each branch of a decision can contain tasks and further decisions.
- Never point an arrow inside another branch.
- Each branch of your program should be covered by a test case.
- It is a good idea to design test cases before implementing a program.

Summary: Boolean

- The type `boolean` has two values, **true** and **false**.
  - Python has two Boolean operators that combine conditions: **and** and **or**.
  - To invert a condition, use the *not* operator.
  - When checking for equality use the `!` operator.
  - The **and** and **or** operators are computed lazily:
    - As soon as the truth value is determined, no further conditions are evaluated.
  - De Morgan's law tells you how to negate **and** and **or** conditions.